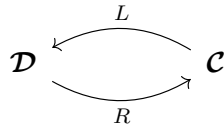


Consider an adjunction  $L \dashv R$



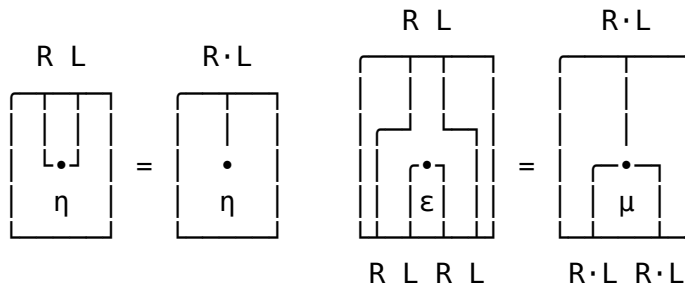
with unit  $\eta : 1_C \Rightarrow R \circ L$  and counit  $\epsilon : L \circ R \Rightarrow 1_D$ , the functors

$$R \circ L : \mathcal{C} \rightarrow \mathcal{C}$$

$$L \circ R : \mathcal{D} \rightarrow \mathcal{D}$$

define

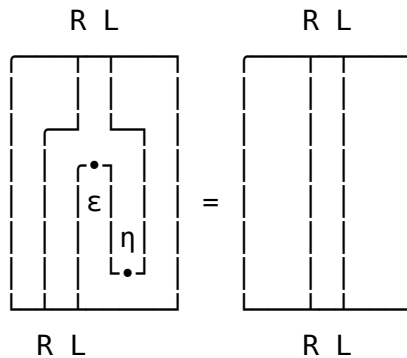
- a monad  $(R \circ L, \eta, R \circ \epsilon \circ L)$



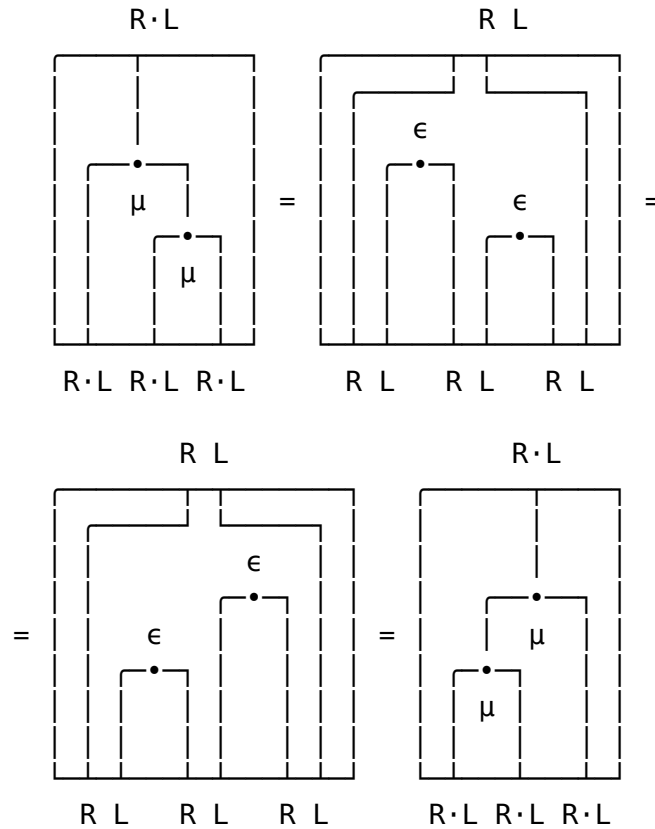
- a comonad  $(L \circ R, \epsilon, L \circ \eta \circ R)$

we have to check the (co)monad laws

- left and right unitality law follows from the snake equalities



- associativity follows from the interchange law



The converse is also true: for any (co)monad there are many adjunctions that generate it.

See [1] and also

- Category Theory III 3.1, Adjunctions and monads - YouTube
- Category Theory III 3.2, Monad Algebras - YouTube

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[1] D. Marsden, *Category Theory Using String Diagrams*, (2014).

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